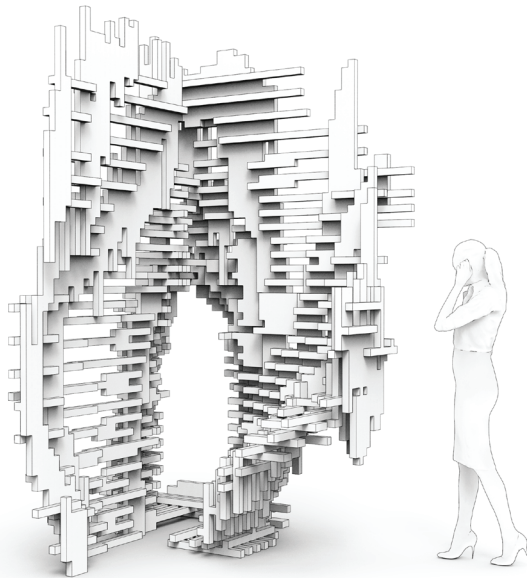


Discrete vs. Discretized Growth

Discretized Fabrication of Geometries Generated With Cellular Growth Simulations



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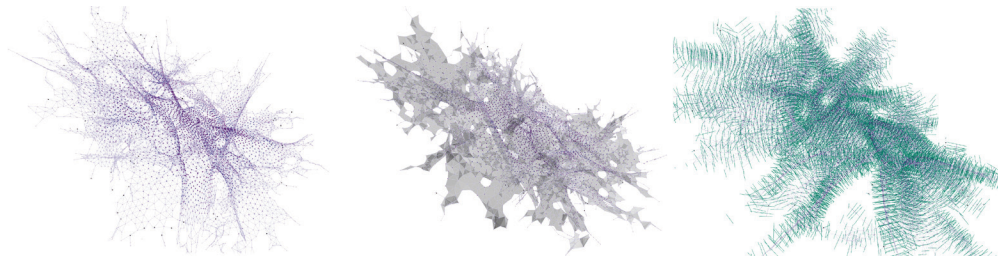
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ABSTRACT

Discrete computational growth simulations, such as Cellular Automata or Diffusion Limited Aggregation, appear to often be difficult to use for architectural design as their geometric outcomes tend to be difficult to control. On the contrary, free-form growth simulations such as Differential Growth or cell-based growth algorithms produce highly complex geometries that are difficult to construct at a larger scale. We therefore propose a methodology of discretized free-form Cellular Growth algorithms in order to utilize the emerging qualities of growth simulations for a feasible architectural design. The methodology has been tested within the framework of a workshop and resulted in the efficient construction of a large physical prototype.

1 Render of Styx Prototype



2 Intercellular behaviors and the resulting data that are used as input parameters for the component placement: Cell Neighborhood, Local Planarity, Cell Orientation.

2

INTRODUCTION

The computational simulation of growth processes has been pursued by different disciplines. In computer science, especially Artificial Life, the aim is to create and understand processes that portray life-like behaviors, while in biology and medicine the focus is on creating models that simulate real-life to a high degree of accuracy.

On the contrary in design, art and architecture, the aim is often to generate new types of geometries with novel, highly complex or aesthetically pleasing characteristics, and in architecture specifically, geometries that may be able to solve specific functional requirements. A growth simulation, with its iterative development towards a larger accumulation of mass, provides the opportunity of an also iterative evaluation of the current state of the geometry, which can then influence the behaviors that guide the growth to develop towards a desirable outcome, on the global as well as local level.

Various types of computational growth simulations have been developed. Due to the algorithmic complexities and the speed of computing, early simulations were often based on calculations within a rectangular grid, such as Diffusion Limited Aggregation (DLA) or Cellular Automata (CA) and Conway's Game of Life. On the contrary, more recent simulations make use of free-form geometry in 3D-space, such as Differential Growth, Cellular Growth algorithms or the CA-based SmoothLife.

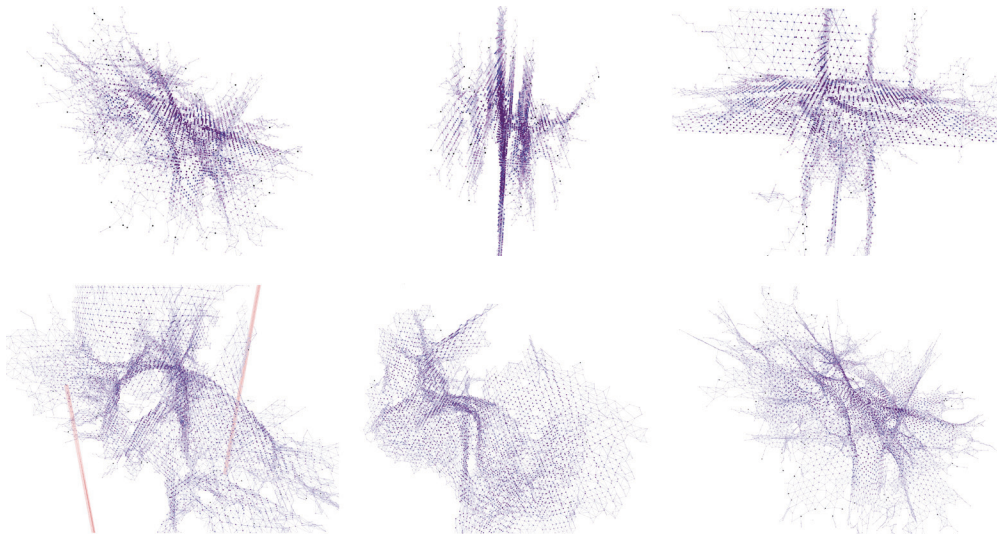
The grid-based simulations can have very simple logics that generate a high degree of complexity and are therefore of great interest to the study of Artificial Life. However, the constraint of the grid results in very specific types of geometries that are usually not suitable for the simulation of biological behaviors, so here the free arrangement of geometry in space is usually used. Also from an architectural perspective, CA and DLA have been used for experimental research projects, but it has been found that the resulting geometries are usually impossible or very difficult to rationalize for real-world projects. The geometries that are generated by the algorithms are hard or

impossible to control, and don't appear to be suitable for addressing functional architectural problems.

In respect to architectural applications, especially if intended for real-world projects, apart from the generation of a functioning geometry also the efficiency and economic buildability are of high importance. Although there have been many advances in construction methods of curved geometry, and the 3D-printing of buildings is in development, economy in today's construction industry is still mostly driven by the use of repetitive elements and mostly rectangular geometries. In terms of buildability, the outcomes of the grid-based algorithms therefore rate much better than the free-form geometries that are generated by the more recently developed algorithms, which usually do not exhibit any repetition at all.

In order to develop growth simulations that can become suitable tools for architectural design, we are therefore proposing the use of discretized Cellular Growth simulations. The algorithm we propose is based on cells that can arrange free in 3D-space and that proliferate based on logics of cell division. The local as well as global behaviors of the cells can be guided through various forces and constraints that are acting on the cells. Although positioned free in space, the cells nevertheless always occupy voxels within an underlying 3D grid. The occupied voxels are then used to define the placement of repetitive components that are assembled to form the final geometry. The placement within the grid allows for further possibilities such as the cells directly reacting towards the grid locations, or the control of component alignment and patternisations.

To test the possibilities of the proposed methodology, we attempted its evaluation on three levels during a design workshop: as an architectural design tool, in an educational setting, and through the physical construction of a 1:1 prototype. During the 9-day workshop, 12 students without prior programming knowledge learned scripting and the logic of the growth algorithm. In groups the students applied the simulations as a design tool. A final 1:1 prototype of 3m height was successfully constructed within 2



3 Global and local forces influencing the resulting geometries. Top: Voxelization. Strata Force. Orthogonal Force. Bottom: Attractor Influences. Undulate Edge Condition. Serrate Edge Condition.

3

days, with the help of a Microsoft HoloLens, a mixed reality headset processing and overlaying construction information into the assembly process.

RELATED WORK

Diffusion Limited Aggregation , Cellular Automata, Conway's Game of Life

Different grid-based mathematical logics have been used to simulate processes of growth. DLA is today often calculated free-form in 3D space, but was originally conceived as working in 2D grids (Witten and Sander 1981).

Sarkar (2000) explains that CA as a generative design tool has been well documented since von Neuman has introduced it in 1963. Especially Conway's Game of Life, a type of CA, has been used to simulate processes of growth (Wolfram 1983, Gardner 1970). Different attempts have been made at utilizing them for architecture and urban design (Al-Qattan, Yan and Galanter 2017, Shiffman 2012, Adilenidou 2015, Kuo and Zausinger 2010).

Although this process can lead to complex geometrical structures derived from simple geometry, Herr and Ford (2007) argue that the transition from a generic CA algorithm to a specific design tool is not very well understood. They argue that CA systems mostly have to undergo multiple adaptations to be able to produce useful outputs in the field architectural design.

In order to overcome the voxelized geometries that result from CA, SmoothLife was developed, a variant that takes into consideration a larger amount of neighboring cells (Rafler 2011, Carroll 2013).

Differential Growth and Cellular Growth

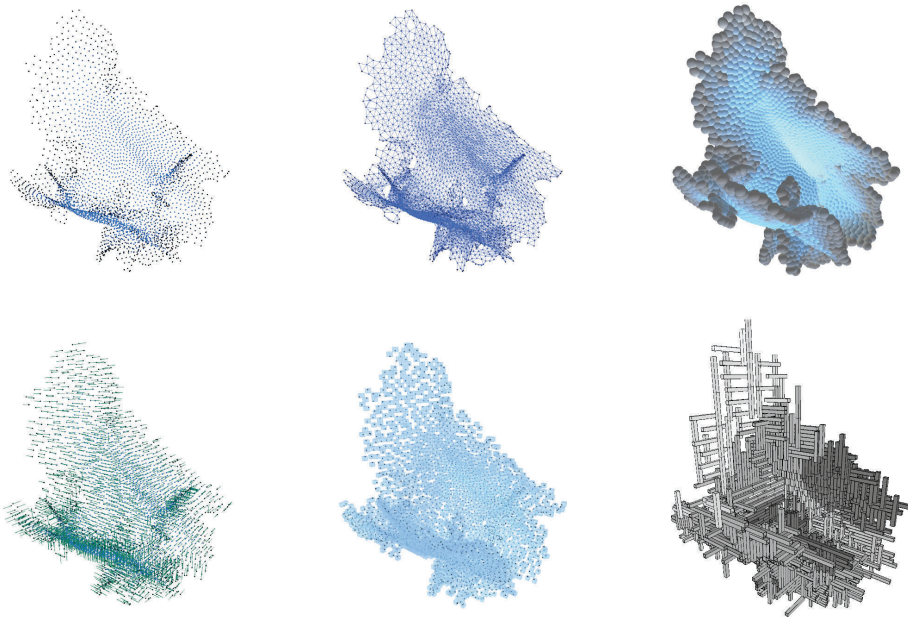
Computational growth simulations based on individual cells are used in developmental biology in order to study the processes that lead to the formation of organisms (Kaandorp et al. 2005, Kaandorp and Kübler 2001, Merks et al 2010, Merks and Glazier 2005, Palm and Merks 2014, Walpole et al. 2013, Wolpert et al. 1998), as well as in cancer research in order to study the growth of tumors (Shirinifard et al. 2009, Milde 2013, Jiao and Torquato 2012, Gevertz and Torquato 2009, Bearer et al. 2009, Neufeld et al. 2013).

In architectural design, Differential Growth simulations have been explored extensively, whereby individual cells can move in 3D space, but are usually arranged as the vertices of polylines or of mesh surfaces. The resulting simulations and free-form geometries have been used for video art or 3D-printed at the small scale (Lomas 2014, Louis-Rosenberg 2015, Bader et al. 2016). A larger installation has been 3D-printed by Alisa Andrasek (Andrasek 2016).

Previous work by the authors utilized a Cellular Growth algorithms, the base algorithm used for the work of this paper, but in a free-form state, to construct an installation from tessellated sheet material (Klemmt and Sugihara 2018).

Discretization for Constructability

The process of discretization as used for the work of this paper, aligns the project within a wider framework of combinatorial and discrete design in architecture. This has been applied to scales ranging from urban design to small scale installations (Kohler 2019, Klemmt et al. 2018).



4 Discretization process and component placement.
Top: Cells. Cell Connections. Solid Volumes.
Bottom: Voxelized Normals. Occupied Voxels. Components.

4

Sanchez (2016) describes this process as a non-parametric approach which focuses on permutation, combination and patterning of discrete units, with part aggregating into larger assemblies, describing meaning, performance and function at different scales of aggregation, leaving the system open-ended, allowing for further expansion and placement of additional parts within.

Retsin (2016a, 2016b) further argues for serial repetition and assembly of discrete parts, based on volume and dissolution of figure, rather than surface and topology typical for parametric projects, emphasizing the importance of part-to-whole relations, and the use of elements which contain a certain kind of design agency, where elements can respond to data such as stress, vector orientation etc.

ALGORITHMIC SIMULATION

Cellular Growth Simulation

The proposed algorithm is based on a point cloud in 3d space, with each cell represented by a point of the point cloud as its center. Iteratively, the cells are evaluated and adjusted by moving their position, and possibly by dividing a cell if certain triggers are met. This leads to an increase of cells over time that take on a geometry based on the various forces that are acting on them, as described in previous papers (Klemmt and Sugihara 2018, Klemmt 2019).

Following an acceleration-velocity model, different forces as vectors are summed up as the cell's acceleration. The acceleration is then added to the cell's velocity, and the

velocity is added to the cell's previous position in order to define its new position. A drag factor of commonly 0.5 is multiplied with the velocity to counteract its otherwise continuous increase from adding the acceleration.

The algorithm starts with a small set of cells that are given initially. In each iteration, a cell first evaluates which other cells it regards as its neighbors, based on proximity and a maximum amount of neighbors. This set of neighbors is then used to calculate intercellular forces between the cells [Figure 2].

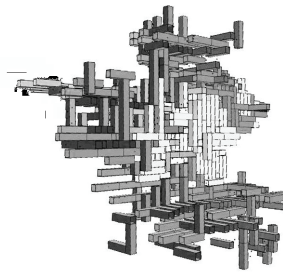
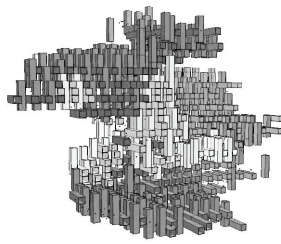
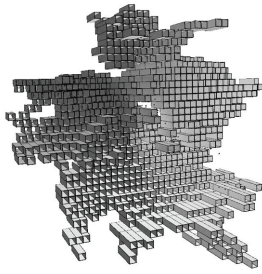
Cell Division

Cells are triggered to divide if they are positioned at the edge of the agglomeration, resulting in a marginal growth of the structure. The cells were identified by their amount of neighbors within a specified range. The cells on the edge will have fewer neighbors than those at the center of the agglomeration. Additionally, cells need to have a minimum age in order to divide.

When a cell divides, a new child cell is inserted close to the parent cell. The child cell inherits the parent's values for various settings, as well as the parent's current neighbors. The age of both parent and child cells are set to 0. Their velocity after the division may be set to move towards or away from their neighbors, resulting in either a smooth or a lobed edge condition.

Cell Forces

In addition to intercellular behaviors, different global forces



5 Different possibilities for component orientation in 1, 2 or 3 axis.

6,7 Elevation and close up renders of the proposal, illustrating patterning and sparsification of the components.

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are acting on the cells causing them to reposition according to their local cell neighborhood. The settings of those forces can be used to control the geometric behaviors as well as the overall arrangement of the cell accumulations [Figure 3].

A point force is calculated between direct neighbors, with the aim of keeping those cells at a defined distance from each other. If the cells are closer than their intended distance, the cells will push each other away; if they are further than this distance they will attract each other. The further two cells are from each other, the attraction between them will diminish.

A planarity force pushes neighboring cells to locally align adjacent to each other in planes. The force is calculated by evaluating the plane that passes through the closest neighbors of a cell, and by then pulling the cell towards this plane.

A strata force causes cells to align in planes that have a globally defined orientation. The normal vector of the planes is given, and a cell is pulled along this vector onto the plane that has its origin at the center of the cell's neighbors.

Globally acting forces are based on attractors and imported geometry that influence the behavior of the cells.

Attractors such as points, lines and surfaces can attract or repel the cells. Different strength / distance profiles can be programmed, and the active range of the attractors can be defined.

Imported mesh geometry can act as attractors. The cells will react to the closest point on the mesh, with similar control over the attractor strength as for the fixed point attractors.

Imported mesh geometries can also act as constraints for the cells. The cells in their movement may be constrained to the inside of a solid mesh, they may be prevented from entering the inside of a solid mesh, or they may be

constrained to move on the surface of a geometry.

Structural Analysis Integration

Structural Analysis was performed using the Karamba tool plugin for Grasshopper, as presented by Preisinger and Heimrath (2014). The advantage of Karamba is to be directly embedded within a parametric environment, and can therefore calculate and evaluate the respective structural setup in real time.

The code was exported in form of a .txt file consisting of the coordinates of the start and end points of the beams in x, y, z direction. This .txt file was read in Rhino Grasshopper and transformed into a structural beam network in Karamba using native components. After adding the material and cross-section properties (40 x 40 mm spruce beams of square shape), a gravity load was applied and the structural calculations were performed. For the scope of the workshop, an optimized geometrical setup was created by taking into account the utilization and deflection values rendered by Karamba.

Discretization and Component Placement

The algorithm calculates with cell locations that are free in space, however, the graphic representation of every cell is then discretized onto a regular square grid. In doing so, the underlying algorithm still has the emergent abilities of the freeform calculations, but its output geometry is voxelized.

The voxelization can be applied to the point representation of the cells, whereby those points are repositioned to their nearest location on the grid. However it is now also possible to draw those voxels as a solid that are occupied by a cell, thereby indicating the volumetric qualities in space that are associated with the cells.

The physical prototype was constructed out of 40mm x 40mm timber beams. A set of components used lengths of this material of 320mm, 480mm and 640mm. Therefore the grid used had an edge length of 40mm, corresponding to the cross section of the material, and accordingly the set of components occupied either 8, 12 or 16 voxels in a row



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adjacent to each other.

For every cell now a component was placed within the grid, through the voxel that was occupied by the cell. During the placement, the voxels of the grid that were occupied by the component were marked, and further components were prevented from being placed if they attempted to use an already occupied voxel [Figure 4].

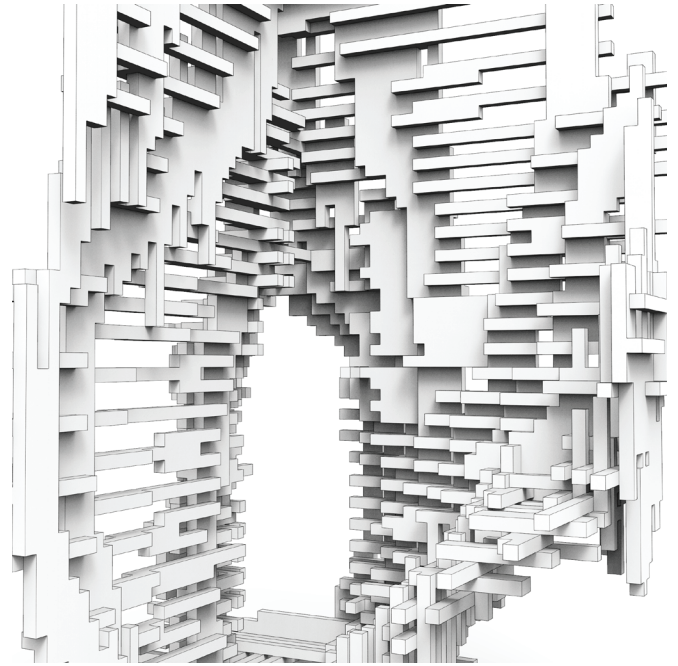
Different possibilities were programmed for the orientation of the components, which can align with the X, the Y or the Z axis of the grid. The components can be placed globally to align with one axis or with two alternating axes, or the components can be aligned according to the local normal direction of each cell, to either most closely align with this normal, or to be placed in line within the surface of the adjacent cells [Figure 5].

Lastly, material densities were controlled through a removal of components, dependent on the proximity of a cell and its component from attractor points in space. This results in a rich pattern design language, able to respond to architectural criteria of porosity, lightness etc [Figure 6 & 7].

PROTOTYPE DESIGN AND CONSTRUCTION

Using Fixed Length as a Measure for Construction Efficiency

The entire construction consisted of 720 overall pieces all equal in width and height (40mm x 40mm). Overall there were nine variations in length (320mm, 480mm, 640mm,



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800mm, 960mm, 1280mm, 600mm, 2080mm, 2240mm).

Wooden beams of the correct cross section were acquired and marked for their intended length. An ordinary jigsaw was used to cut the pieces along their markings. Due to the geometrical simplicity of the individual segments, no additional tools such as CNC machinery was required, and all necessary pieces could be produced in a short time.

The square cross section meant that during the construction process, pieces could not be orientated the wrong way around their length axis. Furthermore, since the offset of two adjacent pieces was always a multiple of the beams cross-section (320mm, 480mm, 640mm), offsets could be easily marked along a segment by any square pieces left over from the initial cutting process.

Materials, Assembly and Construction Process

Before construction, the overall geometry was digitally split into four main pieces and given to student groups for assembly. The solid-wood components were sorted and distributed accordingly. The first step for each group was to create a panel-like part using leftover cutting blocks as separators for the correct offsets between the individual beams. Beams were connected using ordinary SPAX screws and a regular power drill, with the screw length being just under the thickness of two beams. After the construction of the flat panel, the missing pieces were added on the bottom and top accordingly. Finally after the completion of all four pieces, all parts were erected and held in place using bar clamps before being fixated using SPAX screws.



8 Physical 1:1 Prototype

9,10 Details of 1:1 prototype

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Microsoft HoloLens and Fologram - Augmented Reality plug-in for Rhino/Grasshopper were used to enable students to track and supervise the construction process of the four main pieces inside augmented reality (Jahn et al. 2018). Inside the HoloLens the entire part was displayed having beams of different length being represented by different colors. This should ensure that the HoloLens wearing student could quickly instruct his/her peers which beam type had to be placed at what position.

EVALUATION

Architectural Design Possibilities

According to Carroll (2013), "Conway's original game supports an impressive variety of structures, but it's not really robust; if you start with a random configuration, chances are good that it will settle down to something boring before too long." Herr and Ford argue that despite earlier studies that portray CA as generic generative design tools, the transformation from generic CA to specific design tool is not yet well understood, and further that a lack of detailed CA documentation in the field of architectural design has led to a pervasive lack of awareness of such processes among those aiming to apply CA as design tools in architecture (Herr and Ford 2015). While CA and other grid-based growth simulations generate complex

geometry based on simple rules, it appears that their outcomes are often unexpected and difficult to control and are therefore mostly unusable for architectural design. The free-form algorithms on the contrary, while still being able to produce complex geometry, provide much more detailed controls over their outcomes.

The presented project and built installation can be understood as a part of a larger architectural system. The process of form generation is essentially two-fold: The overall form is generated through the cellular growth algorithm, which is then discretized for purpose of fabrication. The methodology therefore draws on the strengths of these two systems.

The Cellular Growth of the underlying surface allows for the generation of spatial enclosures of varying levels of complexities, macro-scale porosity and inter-connectivity. The algorithmic setup, which generates surfaces of different orientations through the previously described cellular forces, can be understood as a tool for the generation of primary architectural elements such as slabs or walls.

The process of discretization acts as a second layer of



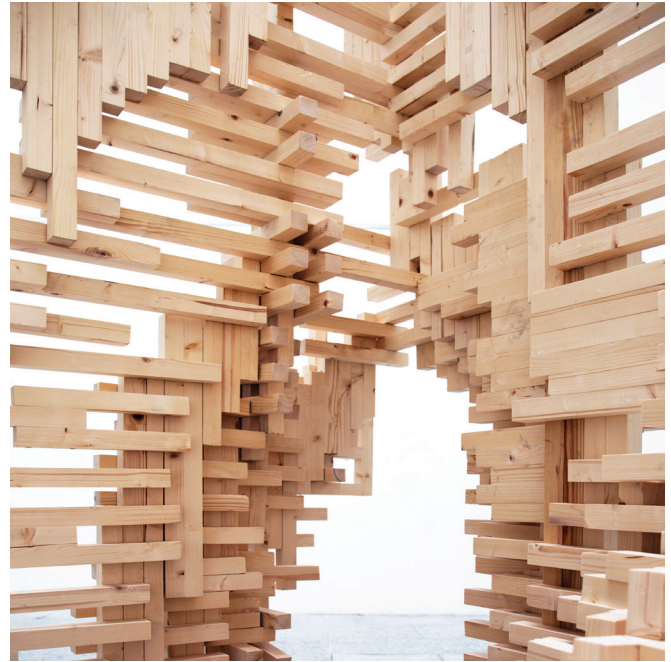
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articulation, assigning meaning to function to enclosed spaces, through the creation of different levels of porosity, openness and patterning. As these aggregations are understood on a volumetric level, and can to a certain degree depart from the underlying surfaces, the architectural qualities of the generated spaces are not strictly bound to the surface topology. If the introduction of porosity might affect the structural performance of a surface, this can be compensated through the introduction of additional elements.

Finally, the system allows for multi-material assemblies in order to create fully functional spaces.

Educational Possibilities

The educational setup was chosen to follow two aims. On one hand, the workshop aimed to educate architecture students towards a critical use of digital technologies. On the other hand it intended to introduce fresh architecture graduates to teaching experiences. According to Menges (2011) and Oxman (2006), prospective architecture professionals are required not only to understand the contemporary digital skill set, but also need to be taught the creative potential and design development mechanism of computational design. A specific design development educational environment, as discussed by Gheorghe (2019) is adapted for this workshop, whereas the participants are introduced in a tutorial style format to state of the art digital tools, while simultaneously having the opportunity to develop in groups their own project ideas under the supervision of the instructors. These projects are discussed



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within the whole group, and one project is selected for further development and full scale fabrication by the complete audience. The students learned the programming of the algorithm and applied it to various design case studies, which were then critically evaluated.

As suggested by Al-Qattan, Yan and Galanter, computer programming is challenging for users because of their difficulty to comprehend its abstract notion, construct algorithms, and envision of the algorithm application in the real world. In architectural education, programming applications present additional level of complexity for designers. (Al-Qattan, Yan and Galanter 2017). Further, Herr and Ford encountered difficulties among students to apply CA as design tools in architecture (Herr and Ford 2015). While the students of our workshop did not all learn programming to a degree where they could develop their own algorithms, all students did receive an in depth introduction, and all students were able to adjust the code and apply it successfully to architectural design.

It was the aim to find the right balance between educational freedom and creativity, user controlled input and semi-random automated process to created sound architectural structure and space. Here, our educational model as applied and described achieves a critical level of production during the week long workshop sufficient for the fabrication of the full scale prototype.

Construction Process

Geometrical features resulting from the use of discrete

components led to a successful prototype built within two days. The voxelization process allowed the use of standard wooden beams as building material, thus saving costs and time since no specialized construction tools or methods were necessary. Designing with repetitive elements led to a small amount in the variation of the component length, therefore speeding up the preparation time when it came to cutting the beams to correct size. The square cross-section of the building material, as well as the fact that components could only be placed along the X, Y or Z direction, made it less likely that during construction elements could be placed or rotated along the wrong axis. Due to the underlying grid, the offset between two adjacent pieces was always a multiple of the cross-section, furthermore preventing the construction team from a wrongful assembly of the prototype.

CONCLUSION AND FUTURE WORK

We regard the combination of the free-form Cellular Growth algorithm with the discretization as a successful tool in order to generate highly complex and reactive geometry that is still easily buildable. The free-form surfaces that a growth algorithm generates are still readable at the large scale, but curvature or geometric details at the voxel or component scale are lost. However, the discretization allows for its own further detailing possibilities through the local positioning and orientation of the individual segments.

In future, an aim is to react in real-time to structural input and adapt the geometry directly within the construction process. Hence, the design process can be optimized to allow a setup with a structural feedback loop, whereby the constructor performs the placement action, the digital Karamba interface re-calculates the structural condition in real-time, and suggests the next placement position, possibly communicated through an augmented reality environment. In such a manner, a direct link between design development and product construction is enabled via the means of digital technologies.

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IMAGE CREDITS

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